

## TD N°03

# LES AUTOMATES À ETATS FINIS (AEF)

### Exercice n°01

Donner sous forme de graphe l'AEF pour chacun des cas suivants:

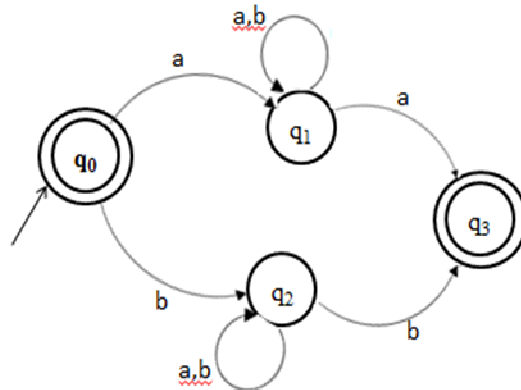
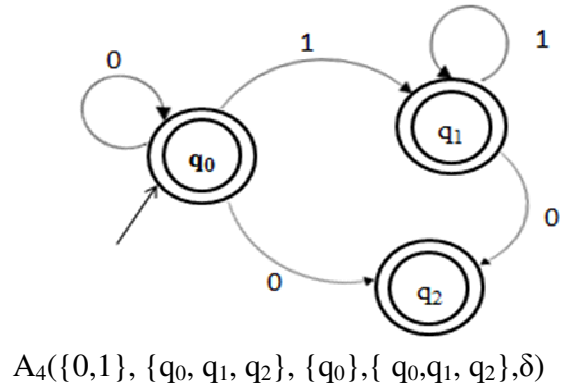
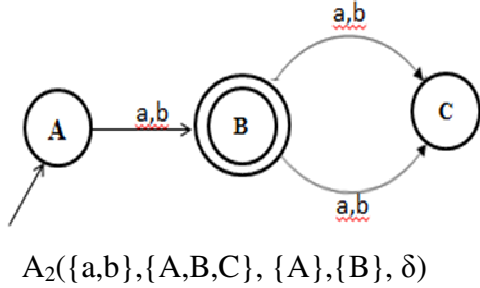
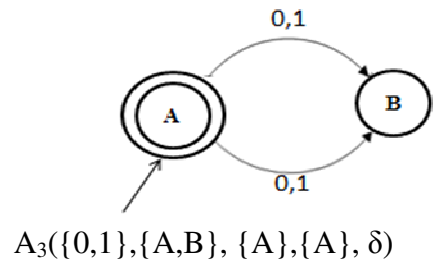
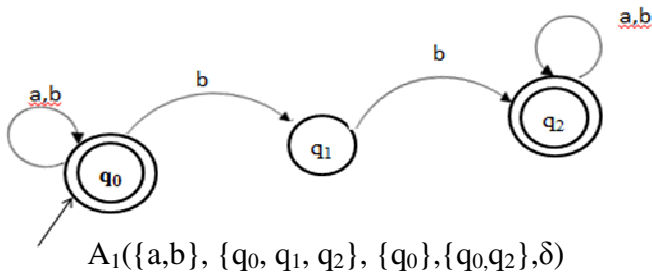
- $G_3 = (\{0,1\}, \{S, A,B,C,D\}, S, R)$ ;  $R = \{S \rightarrow 0A/1B, A \rightarrow 0C/1B/0, B \rightarrow 0A/1D/1, C \rightarrow 0C/1D/0/1, D \rightarrow 0C/1D/0/1\}$
- $ER=(a+b)^*ab(a+b)^*$  (*par intuition*)
- $A_1 (\{a, b\}, \{q_0, q_1, q_2, q_3\}, \{q_0\}, \{q_3\}, \delta)$   
 $\delta (q_0, a) = \{q_1\}$        $\delta (q_0, b) = \{q_2\}$   
 $\delta (q_1, b) = \{q_1\}$        $\delta (q_1, a) = \{q_0, q_1, q_2\}$   
 $\delta (q_2, a) = \{q_2\}$        $\delta (q_2, b) = \{q_2, q_3\}$
- $A_2 (\{1, 2, 3\}, \{q_0, q_1, q_2, q_3, q_4\}, \{q_0\}, \{q_4\}, \delta)$

$\delta$ :

$Q \setminus T$	1	2	3
$\rightarrow q_0$	$\{q_0, q_1\}$	$\{q_0, q_2\}$	-
$q_1$	$\{q_1, q_4\}$	-	$\{q_1\}$
$q_2$	$\{q_2\}$	$\{q_2, q_4\}$	$\{q_2\}$
$q_3$	$\{q_3\}$	$\{q_3\}$	$\{q_3, q_4\}$
$*q_4$	-	-	-

### Exercice n°02

Trouver des expressions régulières pour les AEFs suivants :



### Exercice n°03

Donner les AEFs reconnaissant les langages suivants:

1.  $L_1 = \{a,b\}^* ab \{a,b\}^* \cup \{a,b\}^* bb \{a,b\}^*$
2.  $L_2 = \{w \in \{a,b\}^* / w \text{ se termine par } bab \text{ ou } bb\}$
3. Mot contenant un nombre pair de a
4. Mot contenant un nombre impair de b ainsi que le mot vide.
5.  $L_3 = \{w \in \{0,1\}^* / |w| = 1+4k, k \geq 0\}$

### Exercice n°04

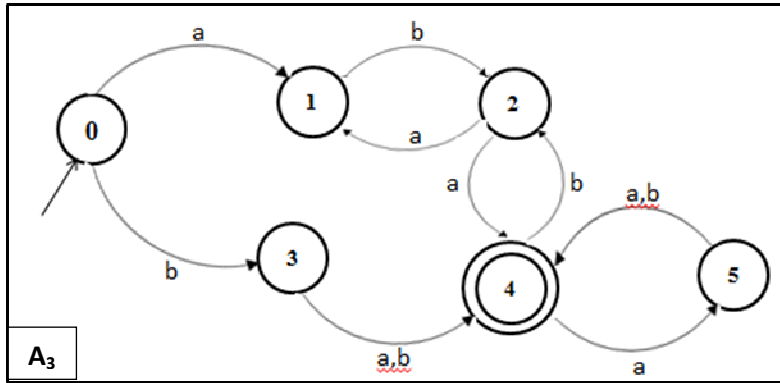
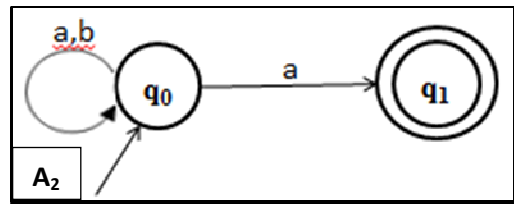
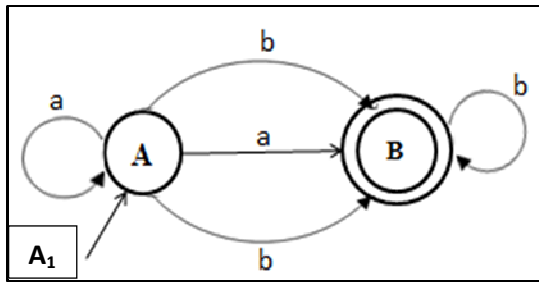
Parmi les AEFs suivants trouver les AEFNDs puis les rendre déterministes:

- 1-  $A_1(\{a,b\}, \{A,B\}, \{A\}, \{B\}, \delta)$
- 2-  $A_2(\{a,b\}, \{q_0, q_1\}, \{q_0\}, \{q_1\}, \delta)$
- 3-  $A_3(\{a,b\}, \{0,1,2,3,4,5\}, \{0\}, \{4\}, \delta)$
- 4-  $A_4(\{a,b\}, \{q_0, q_1, q_2, q_3\}, \{q_0\}, \{q_3\}, \delta)$ 

$\delta(q_0, a) = q_1$	$\delta(q_0, b) = q_2$
$\delta(q_1, a) = \{q_1, q_4\}$	$\delta(q_1, b) = q_1$

$$\delta(q_2, a) = q_2$$

$$\delta(q_2, b) = \{q_2, q_3\}$$

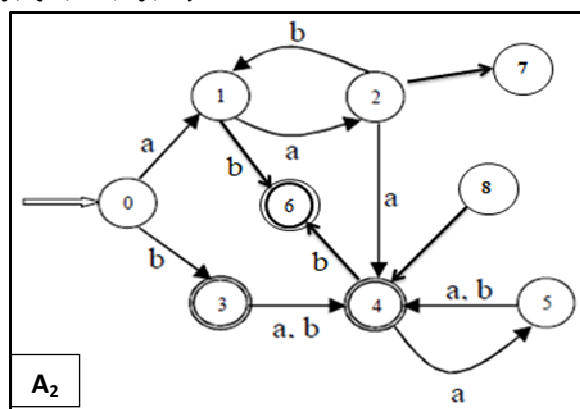
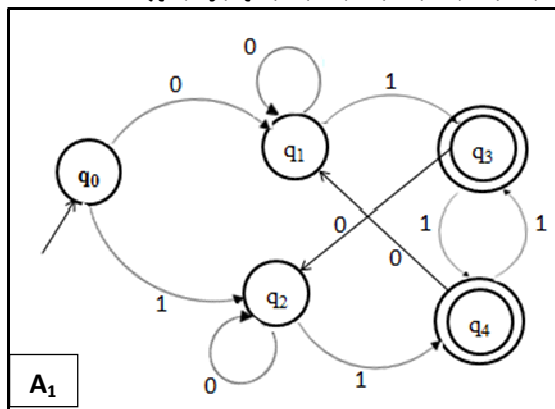


### Exercice n°05

Minimiser les AEFDs suivants :

1-  $A_1(\{0,1\}, \{q_0, q_1, q_2, q_3\}, \{q_0\}, \{q_3, q_4\}, \delta)$

2-  $A_2(\{a,b\}, \{0, 1, 2, 3, 4, 5, 6, 7, 8\}, \{0\}, \{3, 4, 6\}, \delta)$



### Exercice n°06

Soit la grammaire  $G$  suivante :  $G = (\{0, 1\}, \{q_1, q_2, q_3, q_4, q_5\}, q_1, R)$ .

$$R = \{ q_1 \rightarrow 0q_2 / 1q_3;$$

$$q_2 \rightarrow 0q_4 / 1q_3 / 0;$$

$$q_3 \rightarrow 0q_2 / 1q_5 / 1;$$

$$q_4 \rightarrow 0q_4 / 1q_5 / 0 / 1;$$

$$q_5 \rightarrow 0q_4 / 1q_5 / 0 / 1 \}$$

Donner à partir de  $G$  l'automate fini  $A$  associé à  $G$  ?

2. Donner l'automate d'états finis déterministe  $A_1$  équivalent à  $A$  ?

3. Minimiser  $A_1$  ?

3. Soit  $A_2$  l'automate minimal de  $A_1$ . Calculez  $L(A_2)$  ?